

9/28/15 "By failing to prepare, you are preparing to fail" -Ben Franklin

HW: Text page 216 # 42-60 even
Test 2 Wednesday 10/7

AIM: How do we divide complex numbers?

Do Now: rationalize the denominator.

$$\frac{2(2+\sqrt{3})}{(2-\sqrt{3})(2+\sqrt{3})} = \frac{4+2\sqrt{3}}{4+\cancel{2\sqrt{3}}-\cancel{2\sqrt{3}}-3} = \frac{4+2\sqrt{3}}{1}$$

Dividing complex numbers is done similar to rationalizing the denominator

- multiply both numerator and denominator by the conjugate of the denominator
- simplify if possible

$$3) \frac{(2+3i)(1-2i)}{(1+2i)(1-2i)} = \frac{2-4i+3i-6i^2}{1-2i+2i-4i^2} = \frac{2-i+6}{1+4} = \frac{8-i}{5}$$

$$4) \frac{5+10i}{(-2i)(1+2i)} = \frac{5+10i+10i+20i^2}{-2i-2i-4i^2} = \frac{-15+20i}{-4i-4} = \frac{-3+4i}{1}$$

$$5) \frac{10-5i}{2+6i} \cdot \frac{(2-6i)}{(2-6i)} = \frac{20-60i+10i-30i^2}{4-12i+12i-36i^2} = \frac{40-50i}{40} = \frac{-1-7i}{4}$$

$$6) \frac{1(a-bi)}{(a+bi)(a-bi)} = \frac{a-bi}{a^2 - \cancel{abi} + \cancel{abi} - b^2 i^2}$$

$$= \frac{a-bi}{a^2 + b^2}$$

7) What is the multiplicative Inverse of $3+2i$?

$$\text{rule: } \frac{1}{a+bi} = \frac{a-bi}{a^2+b^2}$$

$$\frac{1(3-2i)}{(3+2i)(3-2i)} = \frac{3-2i}{9-6i+6i-4i^2} = \frac{3-2i}{13}$$

$$8) \frac{1}{4-i} = \frac{4+i}{17}$$